

Expression Tree Behavior

- *Expression trees*
 - These trees may be “evaluated” via different traversals
 - ▷ e.g., in-order, post-order, pre-order, level-order
 - The evaluation step may perform various operations... , e.g.,
 - ▷ Traverse and print the expression tree
 - ▷ Return the “value” of the expression tree
 - ▷ Generate code
 - ▷ Perform semantic analysis

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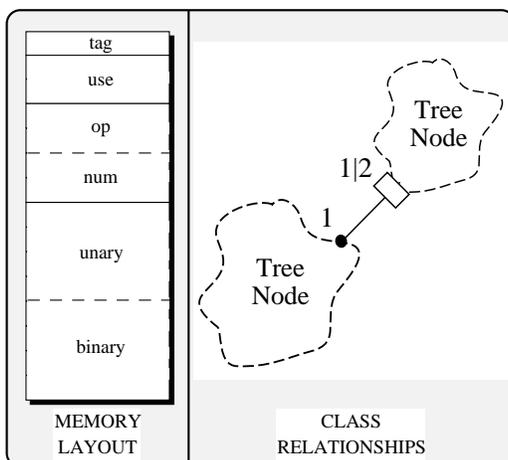
C Version

- A typical functional method for implementing expression trees in C or Ada involves using a **struct/union** to represent data structure, e.g.,

```
typedef struct Tree_Node Tree_Node;
struct Tree_Node {
    enum {
        NUM, UNARY, BINARY
    } tag;
    short use; /* reference count */
    union {
        int num;
        char op[2];
    } o;
#define num o.num
#define op o.op
    union {
        Tree_Node *unary;
        struct { Tree_Node *l, *r; } binary;
    } c;
#define unary c.unary
#define binary c.binary
};
```

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Memory Layout of C Version



- Here’s what the memory layout of a **struct** `Tree_Node` object looks like

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Print_Tree Function

- Typical C or Ada implementation (cont’d)
 - Use a **switch** statement and a recursive function to build and evaluate a tree, e.g.,

```
void print_tree (Tree_Node *root) {
    switch (root->tag) {
        case NUM: cout << root->num; break;
        case UNARY:
            cout << "(" << root->op[0];
            print_tree (root->unary);
            cout << ")"; break;
        case BINARY:
            cout << "(";
            print_tree (root->binary.l);
            cout << root->op[0];
            print_tree (root->binary.r);
            cout << ")"; break;
        default:
            cerr << "error, unknown type\n";
            exit (1);
    }
}
```

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Limitations with C Approach

- Problems or limitations with the typical design and implementation approach include
 - Language feature limitations in C and Ada
 - ▷ *e.g.*, no support for inheritance and dynamic binding
 - Incomplete modeling of the problem domain that results in
 1. Tight coupling between nodes and edges in **union** representation
 2. Complexity being in algorithms rather than the data structures
 - ▷ *e.g.*, **switch** statements are used to select between various types of nodes in the expression trees
 - compare with binary search!
 - ▷ Data structures are “passive” in that functions do most processing work explicitly

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Limitations with C Approach (cont'd)

- Problems with typical approach (cont'd)
 - The program organization makes it difficult to extend, *e.g.*,
 - ▷ Any small changes will ripple through the entire design and implementation
 - *e.g.*, see the ternary extension below
 - ▷ Easy to make mistakes **switching** on type tags. .
 - Solution wastes space by making worst-case assumptions *wrt* **structs** and **unions**
 - ▷ This not essential, but typically occurs
 - ▷ Note that this problem becomes worse the bigger the size of the largest item becomes!

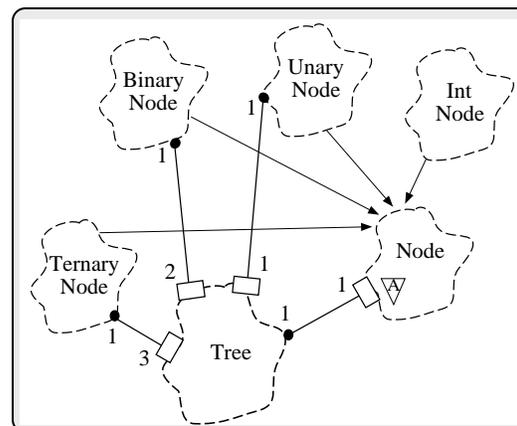
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OO Alternative

- Contrast previous functional approach with an object-oriented decomposition for the same problem:
 - Start with OO modeling of the “expression tree” problem domain:
 - ▷ *e.g.*, go back to original picture
 - There are several classes involved:
 - class** Node: base class that describes expression tree vertices:
 - class** Int_Node: used for implicitly converting **int** to Tree node
 - class** Unary_Node: handles unary operators, *e.g.*, -10 , $+10$, $!a$, or \sim foo, etc.
 - class** Binary_Node: handles binary operators, *e.g.*, $a + b$, $10 - 30$, etc.
 - class** Tree: “glue” code that describes expression tree edges
 - Note, these classes model elements in the problem domain
 - ▷ *i.e.*, nodes and edges (or vertices and arcs)

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Relationships Between Trees and Nodes



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C++ Node Interface

```
• // node.h

#ifndef _NODE_H
#define _NODE_H
#include <stream.h>
#include "tree.h"

/* Describes the Tree vertices */
class Node {
friend class Tree;
friend ostream &operator << (ostream &, const Tree &);

protected: /* only visible to derived classes */
    Node (void): use (1) {}
    // pure virtual
    virtual void print (ostream &) const = 0;
    virtual ~Node (void) {}; // important to make virtual!
private:
    int use; /* reference counter */
};
#endif
```

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C++ Tree Interface

```
• // tree.h

#ifndef _TREE_H
#define _TREE_H
#include "node.h"

/* Describes the Tree edges */
class Tree {
friend class Node;
friend ostream &operator << (ostream &, const Tree &);

public:
    Tree (int);
    Tree (const Tree &t);
    Tree (char *, Tree &);
    Tree (char *, Tree &, Tree &);
    void operator= (const Tree &t);
    virtual ~Tree (void); // important to make virtual
private:
    Node *ptr; /* pointer to a rooted subtree */
};
#endif
```

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C++ Int_Node and Unar_Node Interface

```
• // int-node.h

#ifndef _INT_NODE_H
#define _INT_NODE_H
#include "node.h"
class Int_Node : public Node {
friend class Tree;
private:
    int num; /* operand value */
public:
    Int_Node (int k);
    virtual void print (ostream &stream) const;
};
#endif

• // unary-node.h

#ifndef _UNARY_NODE_H
#define _UNARY_NODE_H
#include "node.h"
class Unary_Node : public Node {
friend class Tree;
public:
    Unary_Node (const char *op, const Tree &t);
    virtual void print (ostream &stream) const;
private:
    const char *operation;
    Tree operand;
};
#endif
```

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C++ Binary_Node Interface

```
• // binary-node.h

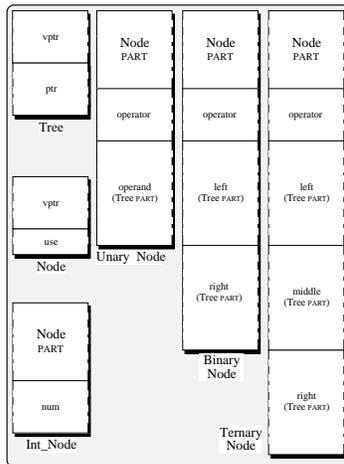
#ifndef _BINARY_NODE_H
#define _BINARY_NODE_H
#include "node.h"

class Binary_Node : public Node {
friend class Tree;

public:
    Binary_Node (const char *op, const Tree &t1,
                const Tree &t2);
    virtual void print (ostream &s) const;
private:
    const char *operation;
    Tree left, right;
};
#endif
```

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Memory Layout for C++ Version



- Memory layouts for different subclasses of Node

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C++ Int_Node and Unary_Node Implementations

- // int-node.C


```
#include "int-node.h"
Int_Node::Int_Node (int k): num (k) { }

void Int_Node::print (ostream &stream) const {
    stream << this->num;
}
```
- // unary-node.C


```
#include "unary-node.h"
Unary_Node::Unary_Node (const char *op, const Tree &t1)
    : operation (op), operand (t1) { }

void Unary_Node::print (ostream &stream) const {
    stream << "(" << this->operation << " "
        << this->operand // recursive call!
        << ")";
}
```

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C++ Binary_Node Implementation

- // binary-node.C


```
#include "binary-node.h"
Binary_Node::Binary_Node (const char *op, const Tree &t1,
    const Tree &t2):
    operation (op), left (t1), right (t2) { }

void Binary_Node::print (ostream &stream) const {
    stream << "(" << this->left // recursive call
        << " " << this->operation
        << " " << this->right // recursive call
        << ")";
}
```

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C++ Tree Implementation

- // tree.C


```
#include "tree.h"
#include "int-node.h"
#include "unary-node.h"
#include "binary-node.h"
#include "ternary-node.h"
Tree::Tree (int num) ptr (new Int_Node (num))
}
Tree::Tree (const Tree &t): ptr (t.ptr)
{ // Sharing, ref-counting.. ++this->ptr->use; }
Tree::Tree (const char *op, const Tree &t)
    : ptr (new Unary_Node (op, t)) {}
Tree::Tree (const char *op, const Tree &t1,
    const Tree &t2):
    : ptr (new Binary_Node (op, t1, t2)) {}
Tree::~Tree (void) { // Ref-counting, garbage collection
    if (--this->ptr->use <= 0)
        delete this->ptr;
}
void Tree::operator= (const Tree &t) {
    ++t.ptr->use;
    if (--this->ptr->use == 0) // order important
        delete this->ptr;
    this->ptr = t.ptr;
}
```

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C++ Main Program

```

• // main.C

#include <stream.h>
#include "tree.h"

ostream &operator<< (ostream &s, const Tree &tree) {
    tree.ptr->print (s); /* Virtual call! */
    /* (*tree->ptr->vptr[1]) (tree->ptr, s);
    return s;
}

int main (void) {
    const Tree t1 = Tree ("*", Tree ("- ", 5),
                        Tree ("+", 3, 4));
    // Tree ("*", Tree ("- ", Tree (5)),
    // Tree ("+", Tree (3), Tree (4)));

    /* prints ((-5) * (3 + 4)) */
    cout << t1 << "\n";
    const Tree t2 = Tree ("*", t1, t1);

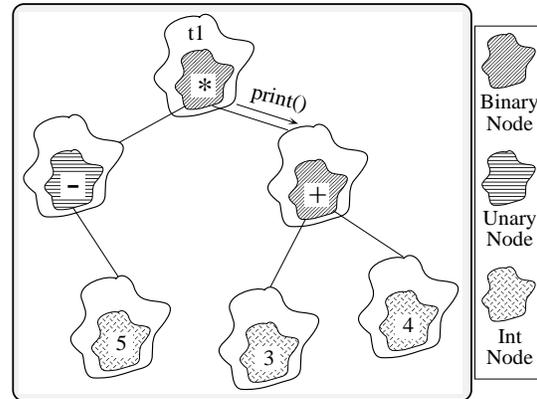
    /* prints (((-5) * (3 + 4)) * ((-5) * (3 + 4))) */
    cout << t2 << "\n";

    /* virtual destructor recursively deletes
    entire tree leaving scope */
}

```

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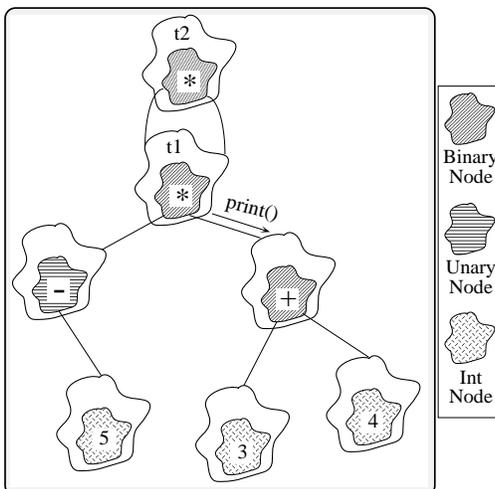
Expression Tree Diagram 1



- Expression tree for t1 = ((-5) * (3 + 4))

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Expression Tree Diagram 2



- Expression tree for t2 = (t1 * t1)

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Extending Solution with Ternary_Nodes

- Extending the existing solution to support ternary nodes is very straight forward

– i.e., just derived new class Ternary_Node

class Ternary_Node: handles ternary operators, e.g., a == b ? c : d, etc.

- // ternary-node.h

```

#ifndef _TERNARY_NODE
#define _TERNARY_NODE
#include "node.h"

```

```

class Ternary_Node : public Node {
friend class Tree;

```

```

private:
    const char *operation;
    Tree left, middle, right;

```

```

public:
    Ternary_Node (const char *, const Tree &,
                 const Tree &, const Tree &);
    virtual void print (ostream &) const;
};
#endif

```

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C++ Ternary_Node Implementation

- // ternary-node.C

```
#include "ternary-node.h"
Ternary_Node::Ternary_Node (const char *op,
                           const Tree &a,
                           const Tree &b,
                           const Tree &c)
    : operation (op), left (a), middle (b), right (c) {}
void Ternary_Node::print (ostream &stream) const {
    stream << this->operation << "("
    << this->left // recursive call
    << "," << this->middle // recursive call
    << "," << this->right // recursive call
    << ")";
}
```

- // Modified class Tree

```
class Tree { // add 1 class constructor
// Same as before
public:
// Same as before
    Tree (const char *, const Tree &,
          const Tree &, const Tree &);
};
Tree::Tree (const char *op, const Tree &a,
            const Tree &b, const Tree &c):
    : ptr (new Ternary_Node (op, a, b, c)) {}
```

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Differences from C Implementation

- On the other hand, modifying the original C approach requires changing:

– The original data structures, e.g.,

```
struct Tree_Node {
    enum {
        NUM, UNARY, BINARY, TERNARY
    } tag;
    // same as before
    union {
        // same as before
        // add this
        struct {
            Tree_Node *l, *m, *r;
        } ternary;
    };
};
```

– and many parts of the code, e.g.,

```
void print_tree (Tree_Node *root) {
    // same as before
    case TERNARY: /* must be TERNARY */
        cout << "(";
        print_tree (root->ternary.l);
        cout << root->op[0];
        print_tree (root->ternary.m);
        cout << root->op[1];
        print_tree (root->ternary.r);
        cout << ")"; break;
    // same as before
}
```

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Summary

- OO version represents a more complete modeling of the problem domain

– e.g., splits data structures into modules that correspond to “objects” and relations in expression trees

- Use of C++ language features simplify the design and facilitate extensibility

– e.g., the original source was hardly affected

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Summary (cont'd)

- Potential Problems with OO approach

– Solution is very “data structure rich”

▷ e.g., Requires configuration management to handle many headers and .C files!

– May be somewhat less efficient than original C approach

▷ e.g., due to virtual function overhead

– In general, however, virtual functions may be no less inefficient than large **switch** statements or **if/else** chains...

– As a rule, be careful of micro vs. macro optimizations

▷ i.e., always profile your code!

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