

Chapter 10

Errata: Volume I: Theory

1. Chapter 4: Page 162: Section: Real Symmetric Generalized Eigenvalue Problems

(a) Line 10: $Ax = \lambda x$ should be $Ax = \lambda Bx$

(b) In Eqn(4.9.11),

$$|\beta_{i+1}| = \|L^{-1}(Av_i - \alpha_i v_i - \beta_i v_{i-1})\|$$

should be

$$|\beta_{i+1}| = \|L^{-1}(Av_i - \alpha_i Bv_i - \beta_i Bv_{i-1})\|$$

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