

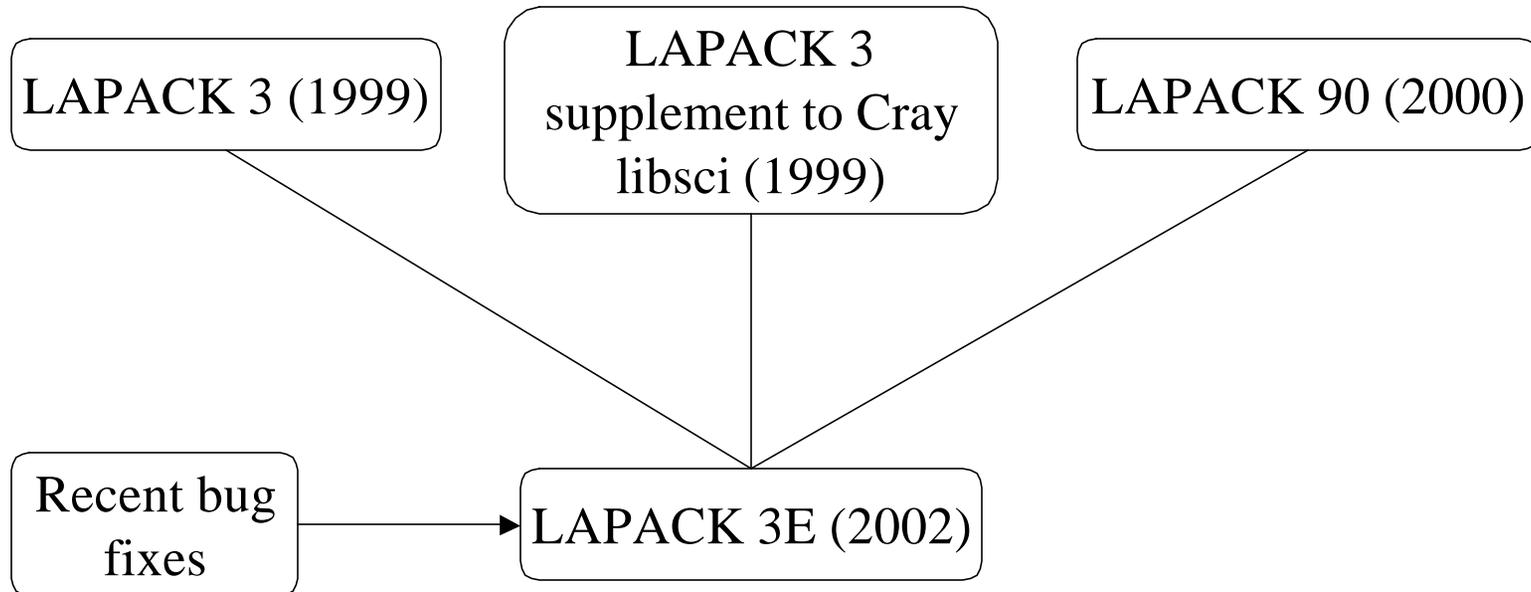
LAPACK 3E – A Fortran 90-enhanced version of LAPACK

Edward Anderson
Lockheed Martin Technology Services
Anderson.Edward@epa.gov

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What is LAPACK 3E?

Project to integrate my past Cray enhancements with LAPACK 3E using LAPACK 90-style generic interfaces



Application

Molecular modeling using methods of computational biophysical chemistry

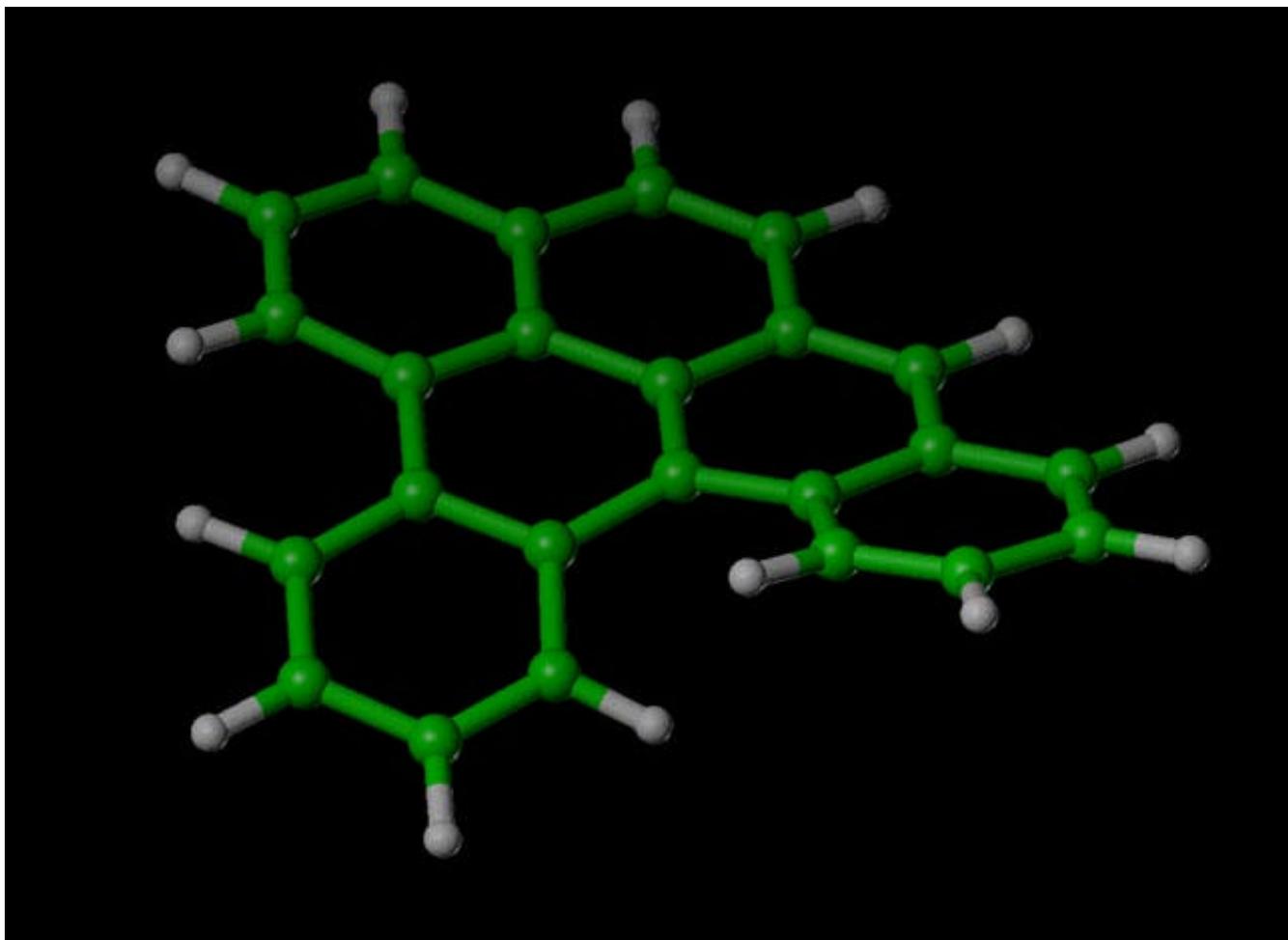
Studying Endocrine Disruptor Chemicals (EDCs) and Polycyclic Aromatic Hydrocarbons (PAHs) formed from incomplete combustion of organic materials

Modeling

- Capacity of metabolites of these environmental chemicals to bind to the ligand binding domain of the estrogen receptor and to DNA
- Effect this binding has on DNA structure

Goal: Assess the risk of cancers of the endocrine system (breast, prostate, thyroid) induced by environmental chemicals

Benzo(a,l)pyrene



Technical approach

- Use semi-empirical Hartree-Fock methods to obtain initial molecular geometries (Gaussian, AMSOL, MOPAC)
- Use ab-initio H-F methods to obtain more complete molecular structures, properties and interaction energies (Gaussian, GAMESS)
- For post H-F calculations, use density functional methods in Gaussian or “Divide and conquer”, a quantum mechanical method for determining the energetic of the binding of environmental molecules to biopolymers

The D&C program uses a recursive bisection method for particle-particle interactions.

It calls LA_SYGVD from LAPACK 90!

LAPACK 95 at NESC

- Cray libsci was based on LAPACK 2.
- I installed LAPACK 3 supplement to libsci and LAPACK 95 on our CRAY T3E.
- Now we want the same libraries on our IBM SP.

Two main issues:

- Libsci supplement used Cray naming conventions (S = 64-bit real, C = 64-bit complex), wanted IEEE conventions on the IBM
- Needed thread-safe version of LAPACK 3 to use shared-memory parallelism

SAVE statements in LAPACK

Two contexts:

- 1) Reverse communication in xLACON and xLASQ3

Add arguments to calling list and rename

- 2) Computed constants, e.g.,

```
LOGICAL FIRST
```

```
DATA FIRST / .TRUE. /
```

```
SAVE FIRST, ...
```

```
IF( FIRST ) THEN
```

```
...
```

```
    FIRST = .FALSE.
```

```
END IF
```

} Compute constants first time
only to reduce overhead

LAPACK 3E design

- Eliminate SAVE statements for thread safety
- Use PARAMETERS for replicated constants
- Parameterize KIND to allow common source for single and double precision
- Use generic interfaces defined in modules for all subroutine calls
- Use preprocessor for renaming at compile time
- Include bug fixes and improvements
- Replicate LAPACK 90 naming conventions

→ Modules and generic interfaces require Fortran 90! ←

Replicated constants

The LAPACK auxiliary routine SLAMCH is called to compute floating point model parameters that are intrinsic in Fortran 90.

$EPS = SLAMCH('Epsilon') \cong EPSILON(1.0)$

$SAFMIN = SLAMCH('Safe minimum') \cong TINY(1.0)$

$SAFMAX = SLAMCH('Overflow') \cong HUGE(1.0)$

SMLNUM is variously computed as

SAFMIN

$SAFMIN * REAL(MAX(1, N))$

$SAFMIN / EPS$

$SAFMIN * (N / EPS)$

$SQRT(SAFMIN / EPS)$

$SQRT(SAFMIN) / EPS$

In LAPACK 3E: make EPS, SAFMIN, etc. all PARAMETERS

Common source for different KINDs

Use KIND-specific declarations:

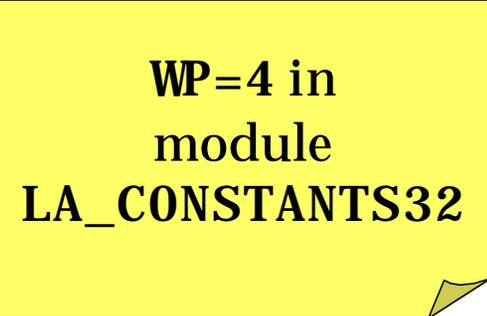
REAL(WP) instead of “REAL” or “DOUBLE PRECISION”

WP is defined in a module:

```
MODULE LA_CONSTANTS  
    INTEGER, PARAMETER :: WP=8  
    . . .  
END MODULE LA_CONSTANTS
```

This module is used in every subroutine:

```
SUBROUTINE SGETRF( ... )  
    USE LA_CONSTANTS  
    . . .
```



**WP=4 in
module
LA_CONSTANTS32**

PARAMETERs in LA_CONSTANTS

WP	EPS, ULP
ZERO, CZERO	SAFMIN
HALF, CHALF	SAFMAX (= 1/SAFMIN)
ONE, CONE	SMLNUM (= SAFMIN/ULP)
TWO	BIGNUM
THREE	RTMIN (= sqrt(SMLNUM))
FOUR	RTMAX
EIGHT	SPREFIX ('S' or 'D')
TEN	CPREFIX ('C' or 'Z')

#i fdef `_CRAY` and **#i fdef** `_CRAYMPP` are used to set numerical constants and subroutine prefixes correctly for Cray architectures

Generic interfaces

Following LAPACK95, create generic interfaces (in a module) for all BLAS and LAPACK routines:

```
MODULE LA_XFOO

INTERFACE LA_FOO

SUBROUTINE SFOO( X )
    USE LA_CONSTANTS32, ONLY: WP
    REAL(WP), INTENT(INOUT) :: X(*)
END SUBROUTINE SFOO

SUBROUTINE DFOO( X )
    USE LA_CONSTANTS, ONLY: WP
    REAL(WP), INTENT(INOUT) :: X(*)
END SUBROUTINE DFOO
```

```
SUBROUTINE CFOO( X )
    USE LA_CONSTANTS32, ONLY: WP
    COMPLEX(WP), INTENT(INOUT) :: X(*)
END SUBROUTINE CFOO

SUBROUTINE ZFOO( X )
    USE LA_CONSTANTS, ONLY: WP
    COMPLEX(WP), INTENT(INOUT) :: X(*)
END SUBROUTINE ZFOO

END INTERFACE ! LA_FOO

END MODULE LA_XFOO
```

Use of generic interfaces

Old style:

```
PROGRAM MAIN  
REAL X(100)  
EXTERNAL SF00  
CALL SF00(X)
```

New style:

```
PROGRAM MAIN  
USE LA_CONSTANTS  
USE LA_XF00  
REAL(WP) :: X(100)  
CALL LA_F00(X)
```

What about:

```
CALL LA_F00(X(10)) !?
```

Mismatched interfaces

The calling site must match one of the interface specs for every argument exactly in type, kind, and rank.

If it doesn't match, you can

- a) Match the interface to the call
- b) Match the call to the interface

LAPACK 3E modules define both the natural interface and a “point” interface for BLAS and LAPACK generic interfaces.

- Natural interface: just like the subroutine definition
- Point interface: all arrays are indexed (such as $A(I, J)$ or $X(1)$)
- If the calling site doesn't match the natural interface, index all the arrays to use the point interface
- Point interface is default – natural interface is a wrapper to it

Point and natural interfaces

Point interfaces allow argument matching by position and type without rank for use with indexed arrays.

```
MODULE LA_XCOPY

INTERFACE LA_COPY

! Point interface for xCOPY1

SUBROUTINE SCOPY1( N, X, Y )
    USE LA_CONSTANTS32, ONLY: WP
    INTEGER, INTENT(IN) :: N
    REAL(WP), INTENT(IN) :: X
    REAL(WP), INTENT(OUT) :: Y
END SUBROUTINE SCOPY1

MODULE PROCEDURE SCOPY1_X1Y1

END INTERFACE ! LA_COPY
PRIVATE SCOPY1_X1Y1
```

```
CONTAINS

! Natural interface for xCOPY1

SUBROUTINE SCOPY1_X1Y1( N, X, Y )
    USE LA_CONSTANTS32, ONLY: WP
    INTEGER, INTENT(IN) :: N
    REAL(WP), INTENT(IN) :: X(*)
    REAL(WP), INTENT(OUT) :: Y(*)
    CALL SCOPY1( N, X(1), Y(1) )
END SUBROUTINE SCOPY1_X1Y1

END MODULE LA_XCOPY
```

Interface modules in LAPACK 3E

- LA_BLAS1
- LA_BLAS2
- LA_BLAS3
- LA_AUXILIARY (commonly used auxiliaries)
- LA_LAPACK (many copied from LAPACK95)
- LA_XYYZZZ (infrequently used auxiliaries)

With USE, I always specify the interfaces needed:

```
USE LA_AUXILIARY, ONLY: I LAENV, XERBLA, LA_LARFG
```

Renaming in the preprocessor

Every LAPACK 3E routine has as its first line

```
#include "lapacknames.inc"
```

The structure of this file is:

```
#if LA_REALSIZE == 4 || LA_REALSIZE == 32
  #ifdef _CRAY
    #define SAXPY HAXPY
    . . .
  #end if
  #define LA_CONSTANTS LA_CONSTANTS32
#else
  #ifndef _CRAY
    #define SAXPY DAXPY
    . . .
  #end if
#endif
```

} S → H and C → G in
32 bits for Cray

} S → D and C → Z in
64 bits for IEEE

Invoking the preprocessor

On Cray, files with .F or .F90 extension invoke the preprocessor:

```
f90 -F -DLA_REALSIZE=4 -o hgetrf.o -c sgetrf.F  
f90 -c sgetrf.F
```

On IBM, files with .F extension invoke the preprocessor:

```
xlf -WF, -DLA_REALSIZE=4 -c sgetrf.F  
xlf -o dgetrf.o -c sgetrf.F
```

Summary of common source changes

```
#include "lapacknames.inc"
    SUBROUTINE SGETRF( M, N, A, LDA, IPIV, INFO )
    USE LA_CONSTANTS
    USE LA_AUXILIARY, ONLY: ILAENV, XERBLA, LA_LASWP
    USE LA_BLAS3, ONLY: LA_GEMM, LA_TRSM
    USE LA_XGETF2
*
* -- LAPACK routine (version 3.0) --
*   Univ. of Tennessee, Univ. of California Berkeley, NAG Ltd.,
*   Courant Institute, Argonne National Lab, and Rice University
*   March 31, 1993
*   04-09-02:  LAPACK 3E version (eca)
*
*   .. Scalar Arguments ..
    INTEGER          INFO, LDA, M, N
*
*   ..
*
*   .. Array Arguments ..
    INTEGER          IPIV( * )
    REAL(WP)         A( LDA, * )
*
*   ..
```

} Translated from
EXTERNAL stmts

```

*      .. Local Scalars ..
      INTEGER          I, IINFO, J, JB, NB
*
*      ..
*      .. Intrinsic Functions ..
      INTRINSIC        MAX, MIN
*
*      ..
*      .. Executable Statements ..
*
      INFO = 0
      IF( M.LT.0 ) THEN
         INFO = -1
      ELSE IF( N.LT.0 ) THEN
         INFO = -2
      ELSE IF( LDA.LT.MAX( 1, M ) ) THEN
         INFO = -4
      END IF
      IF( INFO.NE.0 ) THEN
         CALL XERBLA( SPREFIX // 'GETRF', -INFO )
         RETURN
      END IF
*
*      Quick return if possible
*
      IF( M.EQ.0 .OR. N.EQ.0 )
         $ RETURN

```

} No PARAMETERS and EXTERNAL statements

```

NB = ILAENV( 1, SPREFIX // 'GETRF', ' ', M, N, -1, -1 )
IF( NB.LE.1 .OR. NB.GE.MIN( M, N ) ) THEN
*
*   Use unblocked code.
*
*   CALL LA_GETF2( M, N, A, LDA, IPIV, INFO ) } Natural interface
ELSE
*
*   Use blocked code.
*
DO 20 J = 1, MIN( M, N ), NB
    JB = MIN( MIN( M, N )-J+1, NB )
*
*   Factor diagonal and subdiagonal blocks and test for exact
*   singularity.
*
*   CALL LA_GETF2( M-J+1, JB, A( J, J ), LDA, IPIV( J ), IINFO )
*
*   Adjust INFO and the pivot indices.
*
*   IF( INFO.EQ.0 .AND. IINFO.GT.0 )
$       INFO = IINFO + J - 1
DO 10 I = J, MIN( M, J+JB-1 )
    IPIV( I ) = J - 1 + IPIV( I )
10    CONTINUE
*
*   Apply interchanges to columns 1:J-1.
*
*   CALL LA_LASWP( J-1, A(1,1), LDA, J, J+JB-1, IPIV(1), 1 )

```

Use point interfaces
inside loop for efficiency



```

      IF( J+JB.LE.N ) THEN
*
*       Apply interchanges to columns J+JB:N.
*
      CALL LA_LASWP( N-J-JB+1, A( 1, J+JB ), LDA, J, J+JB-1,
$           IPIV( 1 ), 1 )
*
*       Compute block row of U.
*
      CALL LA_TRSM( 'Left', 'Lower', 'No transpose', 'Unit',
$           JB, N-J-JB+1, ONE, A( J, J ), LDA,
$           A( J, J+JB ), LDA )
      IF( J+JB.LE.M ) THEN
*
*       Update trailing submatrix.
*
      CALL LA_GEMM( 'No transpose', 'No transpose', M-J-JB+1,
$           N-J-JB+1, JB, -ONE, A( J+JB, J ), LDA,
$           A( J, J+JB ), LDA, ONE, A( J+JB, J+JB ), LDA )
      END IF
    END IF
20    CONTINUE
      END IF
      RETURN
      END

```

Mixed interface – convert
to point interface at call



LAWN 126 improvements

LAWN 126 = “Performance improvements to LAPACK for the Cray Scientific Library”, with M. Fahey (1997)

- Parallel linear system solves with NRHS > 1
- Vastly better SLASSQ
- Cleaner SLARTG, SLARFG
- Faster SGEBAL
- Faster SSTEIN (using MGS)
- Add UPLO argument to CPTSV/CTPSVX (only incompatibility with LAPACK 3)
- Call Level 3 LAPACK routines, not Level 2 directly

What's not in LAPACK 3E

- Fortran 90-style argument lists beyond LAPACK 95
- Allocatable work arrays
- Internal subroutines
- New error handler (still using XERBLA)
- Checks for NaN and INF arguments
- Extended precision arithmetic

Current status

- All 655 LAPACK routines converted
- Every routine has a generic INTERFACE
- Compiled successfully on IBM SP and CRAY T3E
- Standard tests pass on IBM SP
- No test routines have been converted
- Will be made available on netlib
- Target availability is September 30, 2002